

1

INTRODUCTION

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2

INTELLIGENT AGENTS

```
function TABLE-DRIVEN-AGENT(percept) returns an action
  persistent: percepts, a sequence, initially empty
               table, a table of actions, indexed by percept sequences, initially fully specified

  append percept to the end of percepts
  action  $\leftarrow$  LOOKUP(percepts, table)
  return action
```

Figure 2.3 The TABLE-DRIVEN-AGENT program is invoked for each new percept and returns an action each time. It retains the complete percept sequence in memory.

```
function REFLEX-VACUUM-AGENT([location, status]) returns an action

  if status = Dirty then return Suck
  else if location = A then return Right
  else if location = B then return Left
```

Figure 2.4 The agent program for a simple reflex agent in the two-state vacuum environment. This program implements the agent function tabulated in Figure ??.

```
function SIMPLE-REFLEX-AGENT(percept) returns an action
  persistent: rules, a set of condition–action rules

  state  $\leftarrow$  INTERPRET-INPUT(percept)
  rule  $\leftarrow$  RULE-MATCH(state, rules)
  action  $\leftarrow$  rule.ACTION
  return action
```

Figure 2.6 A simple reflex agent. It acts according to a rule whose condition matches the current state, as defined by the percept.

```
function MODEL-BASED-REFLEX-AGENT(percept) returns an action
persistent: state, the agent's current conception of the world state
               model, a description of how the next state depends on current state and action
               rules, a set of condition-action rules
               action, the most recent action, initially none

state ← UPDATE-STATE(state, action, percept, model)
rule ← RULE-MATCH(state, rules)
action ← rule.ACTION
return action
```

Figure 2.8 A model-based reflex agent. It keeps track of the current state of the world, using an internal model. It then chooses an action in the same way as the reflex agent.

3

SOLVING PROBLEMS BY SEARCHING

function SIMPLE-PROBLEM-SOLVING-AGENT(*percept*) **returns** an action

persistent: *seq*, an action sequence, initially empty
 state, some description of the current world state
 goal, a goal, initially null
 problem, a problem formulation

state \leftarrow UPDATE-STATE(*state*, *percept*)

if *seq* is empty **then**

goal \leftarrow FORMULATE-GOAL(*state*)

problem \leftarrow FORMULATE-PROBLEM(*state*, *goal*)

seq \leftarrow SEARCH(*problem*)

if *seq* = *failure* **then return** a null action

action \leftarrow FIRST(*seq*)

seq \leftarrow REST(*seq*)

return *action*

Figure 3.1 A simple problem-solving agent. It first formulates a goal and a problem, searches for a sequence of actions that would solve the problem, and then executes the actions one at a time. When this is complete, it formulates another goal and starts over.

```

function TREE-SEARCH(problem) returns a solution, or failure
  initialize the frontier using the initial state of problem
  loop do
    if the frontier is empty then return failure
    choose a leaf node and remove it from the frontier
    if the node contains a goal state then return the corresponding solution
    expand the chosen node, adding the resulting nodes to the frontier

```

```

function GRAPH-SEARCH(problem) returns a solution, or failure
  initialize the frontier using the initial state of problem
  initialize the explored set to be empty
  loop do
    if the frontier is empty then return failure
    choose a leaf node and remove it from the frontier
    if the node contains a goal state then return the corresponding solution
    add the node to the explored set
    expand the chosen node, adding the resulting nodes to the frontier
    only if not in the frontier or explored set

```

Figure 3.7 An informal description of the general tree-search and graph-search algorithms. The parts of GRAPH-SEARCH marked in bold italic are the additions needed to handle repeated states.

```

function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure
  node ← a node with STATE = problem.INITIAL-STATE, PATH-COST = 0
  if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
  frontier ← a FIFO queue with node as the only element
  explored ← an empty set
  loop do
    if EMPTY?(frontier) then return failure
    node ← POP(frontier) /* chooses the shallowest node in frontier */
    add node.STATE to explored
    for each action in problem.ACTIONS(node.STATE) do
      child ← CHILD-NODE(problem, node, action)
      if child.STATE is not in explored or frontier then
        if problem.GOAL-TEST(child.STATE) then return SOLUTION(child)
        frontier ← INSERT(child, frontier)

```

Figure 3.11 Breadth-first search on a graph.

```

function UNIFORM-COST-SEARCH(problem) returns a solution, or failure

  node ← a node with STATE = problem.INITIAL-STATE, PATH-COST = 0
  frontier ← a priority queue ordered by PATH-COST, with node as the only element
  explored ← an empty set
  loop do
    if EMPTY?(frontier) then return failure
    node ← POP(frontier) /* chooses the lowest-cost node in frontier */
    if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
    add node.STATE to explored
    for each action in problem.ACTIONS(node.STATE) do
      child ← CHILD-NODE(problem, node, action)
      if child.STATE is not in explored or frontier then
        frontier ← INSERT(child, frontier)
      else if child.STATE is in frontier with higher PATH-COST then
        replace that frontier node with child

```

Figure 3.13 Uniform-cost search on a graph. The algorithm is identical to the general graph search algorithm in Figure ??, except for the use of a priority queue and the addition of an extra check in case a shorter path to a frontier state is discovered. The data structure for *frontier* needs to support efficient membership testing, so it should combine the capabilities of a priority queue and a hash table.

```

function DEPTH-LIMITED-SEARCH(problem, limit) returns a solution, or failure/cutoff
  return RECURSIVE-DLS(MAKE-NODE(problem.INITIAL-STATE), problem, limit)

function RECURSIVE-DLS(node, problem, limit) returns a solution, or failure/cutoff
  if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
  else if limit = 0 then return cutoff
  else
    cutoff_occurred? ← false
    for each action in problem.ACTIONS(node.STATE) do
      child ← CHILD-NODE(problem, node, action)
      result ← RECURSIVE-DLS(child, problem, limit - 1)
      if result = cutoff then cutoff_occurred? ← true
      else if result ≠ failure then return result
    if cutoff_occurred? then return cutoff else return failure

```

Figure 3.16 A recursive implementation of depth-limited tree search.

```

function ITERATIVE-DEEPENING-SEARCH(problem) returns a solution, or failure
  for depth = 0 to  $\infty$  do
    result  $\leftarrow$  DEPTH-LIMITED-SEARCH(problem, depth)
    if result  $\neq$  cutoff then return result

```

Figure 3.17 The iterative deepening search algorithm, which repeatedly applies depth-limited search with increasing limits. It terminates when a solution is found or if the depth-limited search returns *failure*, meaning that no solution exists.

```

function RECURSIVE-BEST-FIRST-SEARCH(problem) returns a solution, or failure
  return RBFS(problem, MAKE-NODE(problem.INITIAL-STATE),  $\infty$ )

function RBFS(problem, node, f_limit) returns a solution, or failure and a new f-cost limit
  if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
  successors  $\leftarrow$  []
  for each action in problem.ACTIONS(node.STATE) do
    add CHILD-NODE(problem, node, action) into successors
  if successors is empty then return failure,  $\infty$ 
  for each s in successors do /* update f with value from previous search, if any */
    s.f  $\leftarrow$  max(s.g + s.h, node.f)
  loop do
    best  $\leftarrow$  the lowest f-value node in successors
    if best.f > f_limit then return failure, best.f
    alternative  $\leftarrow$  the second-lowest f-value among successors
    result, best.f  $\leftarrow$  RBFS(problem, best, min(f_limit, alternative))
    if result  $\neq$  failure then return result

```

Figure 3.24 The algorithm for recursive best-first search.

4

BEYOND CLASSICAL SEARCH

function HILL-CLIMBING(*problem*) **returns** a state that is a local maximum

```
current ← MAKE-NODE(problem.INITIAL-STATE)
loop do
  neighbor ← a highest-valued successor of current
  if neighbor.VALUE ≤ current.VALUE then return current.STATE
  current ← neighbor
```

Figure 4.2 The hill-climbing search algorithm, which is the most basic local search technique. At each step the current node is replaced by the best neighbor; in this version, that means the neighbor with the highest VALUE, but if a heuristic cost estimate h is used, we would find the neighbor with the lowest h .

function SIMULATED-ANNEALING(*problem*, *schedule*) **returns** a solution state

```
inputs: problem, a problem
        schedule, a mapping from time to “temperature”

current ← MAKE-NODE(problem.INITIAL-STATE)
for  $t = 1$  to  $\infty$  do
   $T \leftarrow \text{schedule}(t)$ 
  if  $T = 0$  then return current
  next ← a randomly selected successor of current
   $\Delta E \leftarrow \text{next}.\text{VALUE} - \text{current}.\text{VALUE}$ 
  if  $\Delta E > 0$  then current ← next
  else current ← next only with probability  $e^{\Delta E/T}$ 
```

Figure 4.5 The simulated annealing algorithm, a version of stochastic hill climbing where some downhill moves are allowed. Downhill moves are accepted readily early in the annealing schedule and then less often as time goes on. The *schedule* input determines the value of the temperature T as a function of time.

function GENETIC-ALGORITHM(*population*, FITNESS-FN) **returns** an individual

inputs: *population*, a set of individuals

FITNESS-FN, a function that measures the fitness of an individual

repeat

new_population \leftarrow empty set

for $i = 1$ **to** SIZE(*population*) **do**

$x \leftarrow$ RANDOM-SELECTION(*population*, FITNESS-FN)

$y \leftarrow$ RANDOM-SELECTION(*population*, FITNESS-FN)

$child \leftarrow$ REPRODUCE(x, y)

if (small random probability) **then** $child \leftarrow$ MUTATE($child$)

 add $child$ to *new_population*

population \leftarrow *new_population*

until some individual is fit enough, or enough time has elapsed

return the best individual in *population*, according to FITNESS-FN

function REPRODUCE(x, y) **returns** an individual

inputs: x, y , parent individuals

$n \leftarrow$ LENGTH(x); $c \leftarrow$ random number from 1 to n

return APPEND(SUBSTRING($x, 1, c$), SUBSTRING($y, c + 1, n$))

Figure 4.8 A genetic algorithm. The algorithm is the same as the one diagrammed in Figure ??, with one variation: in this more popular version, each mating of two parents produces only one offspring, not two.

function AND-OR-GRAPH-SEARCH(*problem*) **returns** a conditional plan, or failure
OR-SEARCH(*problem*.INITIAL-STATE, *problem*, [])

function OR-SEARCH(*state*, *problem*, *path*) **returns** a conditional plan, or failure

if *problem*.GOAL-TEST(*state*) **then return** the empty plan

if *state* is on *path* **then return failure**

for each *action* **in** *problem*.ACTIONS(*state*) **do**

$plan \leftarrow$ AND-SEARCH(RESULTS(*state*, *action*), *problem*, [*state* | *path*])

if $plan \neq failure$ **then return** [*action* | $plan$]

return failure

function AND-SEARCH(*states*, *problem*, *path*) **returns** a conditional plan, or failure

for each s_i **in** *states* **do**

$plan_i \leftarrow$ OR-SEARCH(s_i , *problem*, *path*)

if $plan_i = failure$ **then return failure**

return [**if** s_1 **then** $plan_1$ **else if** s_2 **then** $plan_2$ **else** ... **if** s_{n-1} **then** $plan_{n-1}$ **else** $plan_n$]

Figure 4.11 An algorithm for searching AND-OR graphs generated by nondeterministic environments. It returns a conditional plan that reaches a goal state in all circumstances. (The notation [x | l] refers to the list formed by adding object x to the front of list l .)

```

function ONLINE-DFS-AGENT( $s'$ ) returns an action
  inputs:  $s'$ , a percept that identifies the current state
  persistent: result, a table indexed by state and action, initially empty
               untried, a table that lists, for each state, the actions not yet tried
               unbacktracked, a table that lists, for each state, the backtracks not yet tried
                $s$ ,  $a$ , the previous state and action, initially null

  if GOAL-TEST( $s'$ ) then return stop
  if  $s'$  is a new state (not in untried) then untried[ $s'$ ]  $\leftarrow$  ACTIONS( $s'$ )
  if  $s$  is not null then
    result[ $s$ ,  $a$ ]  $\leftarrow s'$ 
    add  $s$  to the front of unbacktracked[ $s'$ ]
  if untried[ $s'$ ] is empty then
    if unbacktracked[ $s'$ ] is empty then return stop
    else  $a \leftarrow$  an action  $b$  such that result[ $s'$ ,  $b$ ] = POP(unbacktracked[ $s'$ ])
  else  $a \leftarrow$  POP(untried[ $s'$ ])
   $s \leftarrow s'$ 
  return  $a$ 

```

Figure 4.21 An online search agent that uses depth-first exploration. The agent is applicable only in state spaces in which every action can be “undone” by some other action.

```

function LRTA*-AGENT( $s'$ ) returns an action
  inputs:  $s'$ , a percept that identifies the current state
  persistent: result, a table, indexed by state and action, initially empty
                $H$ , a table of cost estimates indexed by state, initially empty
                $s$ ,  $a$ , the previous state and action, initially null

  if GOAL-TEST( $s'$ ) then return stop
  if  $s'$  is a new state (not in  $H$ ) then  $H[s'] \leftarrow h(s')$ 
  if  $s$  is not null
    result[ $s$ ,  $a$ ]  $\leftarrow s'$ 
     $H[s] \leftarrow \min_{b \in \text{ACTIONS}(s)} \text{LRTA}^*\text{-COST}(s, b, \text{result}[s, b], H)$ 
   $a \leftarrow$  an action  $b$  in ACTIONS( $s'$ ) that minimizes  $\text{LRTA}^*\text{-COST}(s', b, \text{result}[s', b], H)$ 
   $s \leftarrow s'$ 
  return  $a$ 

function LRTA*-COST( $s, a, s', H$ ) returns a cost estimate
  if  $s'$  is undefined then return  $h(s)$ 
  else return  $c(s, a, s') + H[s']$ 

```

Figure 4.24 LRTA*-AGENT selects an action according to the values of neighboring states, which are updated as the agent moves about the state space.

5

ADVERSARIAL SEARCH

```
function MINIMAX-DECISION(state) returns an action
  return  $\arg \max_{a \in \text{ACTIONS}(s)} \text{MIN-VALUE}(\text{RESULT}(\text{state}, a))$ 
```

```
function MAX-VALUE(state) returns a utility value
  if TERMINAL-TEST(state) then return UTILITY(state)
   $v \leftarrow -\infty$ 
  for each a in ACTIONS(state) do
     $v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(s, a)))$ 
  return v
```

```
function MIN-VALUE(state) returns a utility value
  if TERMINAL-TEST(state) then return UTILITY(state)
   $v \leftarrow \infty$ 
  for each a in ACTIONS(state) do
     $v \leftarrow \text{MIN}(v, \text{MAX-VALUE}(\text{RESULT}(s, a)))$ 
  return v
```

Figure 5.3 An algorithm for calculating minimax decisions. It returns the action corresponding to the best possible move, that is, the move that leads to the outcome with the best utility, under the assumption that the opponent plays to minimize utility. The functions MAX-VALUE and MIN-VALUE go through the whole game tree, all the way to the leaves, to determine the backed-up value of a state. The notation $\arg \max_{a \in S} f(a)$ computes the element *a* of set *S* that has the maximum value of *f(a)*.

function ALPHA-BETA-SEARCH(*state*) **returns** an action
 $v \leftarrow \text{MAX-VALUE}(\text{state}, -\infty, +\infty)$
return the *action* in ACTIONS(*state*) with value *v*

function MAX-VALUE(*state*, α , β) **returns** a utility value
if TERMINAL-TEST(*state*) **then return** UTILITY(*state*)
 $v \leftarrow -\infty$
for each *a* **in** ACTIONS(*state*) **do**
 $v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(s, a), \alpha, \beta))$
if $v \geq \beta$ **then return** *v*
 $\alpha \leftarrow \text{MAX}(\alpha, v)$
return *v*

function MIN-VALUE(*state*, α , β) **returns** a utility value
if TERMINAL-TEST(*state*) **then return** UTILITY(*state*)
 $v \leftarrow +\infty$
for each *a* **in** ACTIONS(*state*) **do**
 $v \leftarrow \text{MIN}(v, \text{MAX-VALUE}(\text{RESULT}(s, a), \alpha, \beta))$
if $v \leq \alpha$ **then return** *v*
 $\beta \leftarrow \text{MIN}(\beta, v)$
return *v*

Figure 5.7 The alpha-beta search algorithm. Notice that these routines are the same as the MINIMAX functions in Figure ??, except for the two lines in each of MIN-VALUE and MAX-VALUE that maintain α and β (and the bookkeeping to pass these parameters along).

6

CONSTRAINT SATISFACTION PROBLEMS

```
function AC-3(csp) returns false if an inconsistency is found and true otherwise
inputs: csp, a binary CSP with components ( $X, D, C$ )
local variables: queue, a queue of arcs, initially all the arcs in csp

while queue is not empty do
    ( $X_i, X_j$ )  $\leftarrow$  REMOVE-FIRST(queue)
    if REVISE(csp,  $X_i, X_j$ ) then
        if size of  $D_i$  = 0 then return false
        for each  $X_k$  in  $X_i$ .NEIGHBORS -  $\{X_j\}$  do
            add ( $X_k, X_i$ ) to queue
return true
```

```
function REVISE(csp,  $X_i, X_j$ ) returns true iff we revise the domain of  $X_i$ 
    revised  $\leftarrow$  false
    for each  $x$  in  $D_i$  do
        if no value  $y$  in  $D_j$  allows ( $x, y$ ) to satisfy the constraint between  $X_i$  and  $X_j$  then
            delete  $x$  from  $D_i$ 
            revised  $\leftarrow$  true
    return revised
```

Figure 6.3 The arc-consistency algorithm AC-3. After applying AC-3, either every arc is arc-consistent, or some variable has an empty domain, indicating that the CSP cannot be solved. The name “AC-3” was used by the algorithm’s inventor (?) because it’s the third version developed in the paper.

```

function BACKTRACKING-SEARCH(csp) returns a solution, or failure
    return BACKTRACK({ }, csp)

function BACKTRACK(assignment, csp) returns a solution, or failure
    if assignment is complete then return assignment
    var ← SELECT-UNASSIGNED-VARIABLE(csp)
    for each value in ORDER-DOMAIN-VALUES(var, assignment, csp) do
        if value is consistent with assignment then
            add {var = value} to assignment
            inferences ← INFERENCE(csp, var, value)
            if inferences ≠ failure then
                add inferences to assignment
                result ← BACKTRACK(assignment, csp)
                if result ≠ failure then
                    return result
            remove {var = value} and inferences from assignment
    return failure

```

Figure 6.5 A simple backtracking algorithm for constraint satisfaction problems. The algorithm is modeled on the recursive depth-first search of Chapter ?? . By varying the functions SELECT-UNASSIGNED-VARIABLE and ORDER-DOMAIN-VALUES, we can implement the general-purpose heuristics discussed in the text. The function INFERENCE can optionally be used to impose arc-, path-, or k -consistency, as desired. If a value choice leads to failure (noticed either by INFERENCE or by BACKTRACK), then value assignments (including those made by INFERENCE) are removed from the current assignment and a new value is tried.

```

function MIN-CONFLICTS(csp, max_steps) returns a solution or failure
    inputs: csp, a constraint satisfaction problem
            max_steps, the number of steps allowed before giving up

    current ← an initial complete assignment for csp
    for  $i = 1$  to max_steps do
        if current is a solution for csp then return current
        var ← a randomly chosen conflicted variable from csp.VARIABLES
        value ← the value  $v$  for var that minimizes CONFLICTS(var,  $v$ , current, csp)
        set var = value in current
    return failure

```

Figure 6.8 The MIN-CONFLICTS algorithm for solving CSPs by local search. The initial state may be chosen randomly or by a greedy assignment process that chooses a minimal-conflict value for each variable in turn. The CONFLICTS function counts the number of constraints violated by a particular value, given the rest of the current assignment.

```

function TREE-CSP-SOLVER(csp) returns a solution, or failure
  inputs: csp, a CSP with components X, D, C

  n ← number of variables in X
  assignment ← an empty assignment
  root ← any variable in X
  X ← TOPOLOGICALSORT(X, root)
  for j = n down to 2 do
    MAKE-ARC-CONSISTENT(PARENT(Xj), Xj)
    if it cannot be made consistent then return failure
  for i = 1 to n do
    assignment[Xi] ← any consistent value from Di
    if there is no consistent value then return failure
  return assignment

```

Figure 6.11 The TREE-CSP-SOLVER algorithm for solving tree-structured CSPs. If the CSP has a solution, we will find it in linear time; if not, we will detect a contradiction.

7

LOGICAL AGENTS

function KB-AGENT(*percept*) **returns** an *action*
persistent: *KB*, a knowledge base
 t, a counter, initially 0, indicating time

TELL(*KB*, MAKE-PERCEPT-SENTENCE(*percept*, *t*))
action \leftarrow ASK(*KB*, MAKE-ACTION-QUERY(*t*))
TELL(*KB*, MAKE-ACTION-SENTENCE(*action*, *t*))
t \leftarrow *t* + 1
return *action*

Figure 7.1 A generic knowledge-based agent. Given a percept, the agent adds the percept to its knowledge base, asks the knowledge base for the best action, and tells the knowledge base that it has in fact taken that action.

```

function TT-ENTAILS?( $KB, \alpha$ ) returns true or false
  inputs:  $KB$ , the knowledge base, a sentence in propositional logic
            $\alpha$ , the query, a sentence in propositional logic

   $symbols \leftarrow$  a list of the proposition symbols in  $KB$  and  $\alpha$ 
  return TT-CHECK-ALL( $KB, \alpha, symbols, \{ \}$ )

```

```

function TT-CHECK-ALL( $KB, \alpha, symbols, model$ ) returns true or false
  if EMPTY?( $symbols$ ) then
    if PL-TRUE?( $KB, model$ ) then return PL-TRUE?( $\alpha, model$ )
    else return true // when  $KB$  is false, always return true
  else do
     $P \leftarrow$  FIRST( $symbols$ )
     $rest \leftarrow$  REST( $symbols$ )
    return (TT-CHECK-ALL( $KB, \alpha, rest, model \cup \{P = true\}$ )
           and
           TT-CHECK-ALL( $KB, \alpha, rest, model \cup \{P = false\}$ ))

```

Figure 7.8 A truth-table enumeration algorithm for deciding propositional entailment. (TT stands for truth table.) PL-TRUE? returns *true* if a sentence holds within a model. The variable *model* represents a partial model—an assignment to some of the symbols. The keyword “**and**” is used here as a logical operation on its two arguments, returning *true* or *false*.

```

function PL-RESOLUTION( $KB, \alpha$ ) returns true or false
  inputs:  $KB$ , the knowledge base, a sentence in propositional logic
            $\alpha$ , the query, a sentence in propositional logic

   $clauses \leftarrow$  the set of clauses in the CNF representation of  $KB \wedge \neg \alpha$ 
   $new \leftarrow \{ \}$ 
  loop do
    for each pair of clauses  $C_i, C_j$  in  $clauses$  do
       $resolvents \leftarrow$  PL-RESOLVE( $C_i, C_j$ )
      if  $resolvents$  contains the empty clause then return true
       $new \leftarrow new \cup resolvents$ 
    if  $new \subseteq clauses$  then return false
   $clauses \leftarrow clauses \cup new$ 

```

Figure 7.9 A simple resolution algorithm for propositional logic. The function PL-RESOLVE returns the set of all possible clauses obtained by resolving its two inputs.

```

function PL-FC-ENTAILS?(KB, q) returns true or false
  inputs: KB, the knowledge base, a set of propositional definite clauses
           q, the query, a proposition symbol
  count  $\leftarrow$  a table, where count[c] is the number of symbols in c's premise
  inferred  $\leftarrow$  a table, where inferred[s] is initially false for all symbols
  agenda  $\leftarrow$  a queue of symbols, initially symbols known to be true in KB

  while agenda is not empty do
    p  $\leftarrow$  POP(agenda)
    if p = q then return true
    if inferred[p] = false then
      inferred[p]  $\leftarrow$  true
      for each clause c in KB where p is in c.PREMISE do
        decrement count[c]
        if count[c] = 0 then add c.CONCLUSION to agenda
  return false

```

Figure 7.12 The forward-chaining algorithm for propositional logic. The *agenda* keeps track of symbols known to be true but not yet “processed.” The *count* table keeps track of how many premises of each implication are as yet unknown. Whenever a new symbol *p* from the agenda is processed, the count is reduced by one for each implication in whose premise *p* appears (easily identified in constant time with appropriate indexing.) If a count reaches zero, all the premises of the implication are known, so its conclusion can be added to the agenda. Finally, we need to keep track of which symbols have been processed; a symbol that is already in the set of inferred symbols need not be added to the agenda again. This avoids redundant work and prevents loops caused by implications such as $P \Rightarrow Q$ and $Q \Rightarrow P$.

```

function DPLL-SATISFIABLE?(s) returns true or false
  inputs: s, a sentence in propositional logic

  clauses  $\leftarrow$  the set of clauses in the CNF representation of s
  symbols  $\leftarrow$  a list of the proposition symbols in s
  return DPLL(clauses, symbols, { })

```

```

function DPLL(clauses, symbols, model) returns true or false

  if every clause in clauses is true in model then return true
  if some clause in clauses is false in model then return false
  P, value  $\leftarrow$  FIND-PURE-SYMBOL(symbols, clauses, model)
  if P is non-null then return DPLL(clauses, symbols – P, model  $\cup$  {P=value})
  P, value  $\leftarrow$  FIND-UNIT-CLAUSE(clauses, model)
  if P is non-null then return DPLL(clauses, symbols – P, model  $\cup$  {P=value})
  P  $\leftarrow$  FIRST(symbols); rest  $\leftarrow$  REST(symbols)
  return DPLL(clauses, rest, model  $\cup$  {P=true}) or
    DPLL(clauses, rest, model  $\cup$  {P=false})

```

Figure 7.14 The DPLL algorithm for checking satisfiability of a sentence in propositional logic. The ideas behind FIND-PURE-SYMBOL and FIND-UNIT-CLAUSE are described in the text; each returns a symbol (or null) and the truth value to assign to that symbol. Like TT-ENTAILS?, DPLL operates over partial models.

```

function WALKSAT(clauses, p, max_flips) returns a satisfying model or failure
  inputs: clauses, a set of clauses in propositional logic
           p, the probability of choosing to do a “random walk” move, typically around 0.5
           max_flips, number of flips allowed before giving up

  model  $\leftarrow$  a random assignment of true/false to the symbols in clauses
  for i = 1 to max_flips do
    if model satisfies clauses then return model
    clause  $\leftarrow$  a randomly selected clause from clauses that is false in model
    with probability p flip the value in model of a randomly selected symbol from clause
    else flip whichever symbol in clause maximizes the number of satisfied clauses
  return failure

```

Figure 7.15 The WALKSAT algorithm for checking satisfiability by randomly flipping the values of variables. Many versions of the algorithm exist.

```

function HYBRID-WUMPUS-AGENT(percept) returns an action
  inputs: percept, a list, [stench, breeze, glitter, bump, scream]
  persistent: KB, a knowledge base, initially the atemporal “wumpus physics”
               t, a counter, initially 0, indicating time
               plan, an action sequence, initially empty

  TELL(KB, MAKE-PERCEPT-SENTENCE(percept, t))
  TELL the KB the temporal “physics” sentences for time t
  safe  $\leftarrow \{[x, y] : \text{ASK}(\text{KB}, \text{OK}_{x,y}^t) = \text{true}\}$ 
  if ASK(KB, Glittert) = true then
    plan  $\leftarrow [\text{Grab}] + \text{PLAN-ROUTE}(\text{current}, \{[1,1]\}, \text{safe}) + [\text{Climb}]$ 
  if plan is empty then
    unvisited  $\leftarrow \{[x, y] : \text{ASK}(\text{KB}, L_{x,y}^{t'}) = \text{false} \text{ for all } t' \leq t\}$ 
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \text{unvisited} \cap \text{safe}, \text{safe})$ 
  if plan is empty and ASK(KB, HaveArrowt) = true then
    possible_wumpus  $\leftarrow \{[x, y] : \text{ASK}(\text{KB}, \neg W_{x,y}) = \text{false}\}$ 
    plan  $\leftarrow \text{PLAN-SHOT}(\text{current}, \text{possible\_wumpus}, \text{safe})$ 
  if plan is empty then // no choice but to take a risk
    not_unsafe  $\leftarrow \{[x, y] : \text{ASK}(\text{KB}, \neg \text{OK}_{x,y}^t) = \text{false}\}$ 
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \text{unvisited} \cap \text{not\_unsafe}, \text{safe})$ 
  if plan is empty then
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \{[1, 1]\}, \text{safe}) + [\text{Climb}]$ 
  action  $\leftarrow \text{POP}(\text{plan})$ 
  TELL(KB, MAKE-ACTION-SENTENCE(action, t))
  t  $\leftarrow t + 1$ 
  return action

```

```

function PLAN-ROUTE(current, goals, allowed) returns an action sequence
  inputs: current, the agent’s current position
          goals, a set of squares; try to plan a route to one of them
          allowed, a set of squares that can form part of the route

  problem  $\leftarrow \text{ROUTE-PROBLEM}(\text{current}, \text{goals}, \text{allowed})$ 
  return A*-GRAPH-SEARCH(problem)

```

Figure 7.17 A hybrid agent program for the wumpus world. It uses a propositional knowledge base to infer the state of the world, and a combination of problem-solving search and domain-specific code to decide what actions to take.

```

function SATPLAN(init, transition, goal,  $T_{\max}$ ) returns solution or failure
inputs: init, transition, goal, constitute a description of the problem
          $T_{\max}$ , an upper limit for plan length

for  $t = 0$  to  $T_{\max}$  do
     $cnf \leftarrow$  TRANSLATE-TO-SAT(init, transition, goal,  $t$ )
     $model \leftarrow$  SAT-SOLVER( $cnf$ )
    if  $model$  is not null then
        return EXTRACT-SOLUTION( $model$ )
return failure

```

Figure 7.19 The SATPLAN algorithm. The planning problem is translated into a CNF sentence in which the goal is asserted to hold at a fixed time step t and axioms are included for each time step up to t . If the satisfiability algorithm finds a model, then a plan is extracted by looking at those proposition symbols that refer to actions and are assigned *true* in the model. If no model exists, then the process is repeated with the goal moved one step later.

8

FIRST-ORDER LOGIC

9

INFERENCE IN FIRST-ORDER LOGIC

```
function UNIFY( $x, y, \theta$ ) returns a substitution to make  $x$  and  $y$  identical
  inputs:  $x$ , a variable, constant, list, or compound expression
            $y$ , a variable, constant, list, or compound expression
            $\theta$ , the substitution built up so far (optional, defaults to empty)

  if  $\theta = \text{failure}$  then return failure
  else if  $x = y$  then return  $\theta$ 
  else if VARIABLE?( $x$ ) then return UNIFY-VAR( $x, y, \theta$ )
  else if VARIABLE?( $y$ ) then return UNIFY-VAR( $y, x, \theta$ )
  else if COMPOUND?( $x$ ) and COMPOUND?( $y$ ) then
    return UNIFY( $x$ .ARGS,  $y$ .ARGS, UNIFY( $x$ .OP,  $y$ .OP,  $\theta$ ))
  else if LIST?( $x$ ) and LIST?( $y$ ) then
    return UNIFY( $x$ .REST,  $y$ .REST, UNIFY( $x$ .FIRST,  $y$ .FIRST,  $\theta$ ))
  else return failure
```

```
function UNIFY-VAR( $var, x, \theta$ ) returns a substitution

  if  $\{var/val\} \in \theta$  then return UNIFY( $val, x, \theta$ )
  else if  $\{x/val\} \in \theta$  then return UNIFY( $var, val, \theta$ )
  else if OCCUR-CHECK?( $var, x$ ) then return failure
  else return add  $\{var/x\}$  to  $\theta$ 
```

Figure 9.1 The unification algorithm. The algorithm works by comparing the structures of the inputs, element by element. The substitution θ that is the argument to UNIFY is built up along the way and is used to make sure that later comparisons are consistent with bindings that were established earlier. In a compound expression such as $F(A, B)$, the OP field picks out the function symbol F and the ARGS field picks out the argument list (A, B) .


```

function FOL-FC-ASK( $KB, \alpha$ ) returns a substitution or false
  inputs:  $KB$ , the knowledge base, a set of first-order definite clauses
            $\alpha$ , the query, an atomic sentence
  local variables: new, the new sentences inferred on each iteration

  repeat until new is empty
     $new \leftarrow \{ \}$ 
    for each rule in  $KB$  do
       $(p_1 \wedge \dots \wedge p_n \Rightarrow q) \leftarrow \text{STANDARDIZE-VARIABLES}(\text{rule})$ 
      for each  $\theta$  such that  $\text{SUBST}(\theta, p_1 \wedge \dots \wedge p_n) = \text{SUBST}(\theta, p'_1 \wedge \dots \wedge p'_n)$ 
        for some  $p'_1, \dots, p'_n$  in  $KB$ 
         $q' \leftarrow \text{SUBST}(\theta, q)$ 
        if  $q'$  does not unify with some sentence already in  $KB$  or new then
          add  $q'$  to new
           $\phi \leftarrow \text{UNIFY}(q', \alpha)$ 
          if  $\phi$  is not fail then return  $\phi$ 
    add new to  $KB$ 
  return false

```

Figure 9.3 A conceptually straightforward, but very inefficient, forward-chaining algorithm. On each iteration, it adds to KB all the atomic sentences that can be inferred in one step from the implication sentences and the atomic sentences already in KB . The function STANDARDIZE-VARIABLES replaces all variables in its arguments with new ones that have not been used before.

```

function FOL-BC-ASK( $KB, query$ ) returns a generator of substitutions
  return FOL-BC-OR( $KB, query, \{ \}$ )

```

```

generator FOL-BC-OR( $KB, goal, \theta$ ) yields a substitution
  for each rule  $(lhs \Rightarrow rhs)$  in FETCH-RULES-FOR-GOAL( $KB, goal$ ) do
     $(lhs, rhs) \leftarrow \text{STANDARDIZE-VARIABLES}((lhs, rhs))$ 
    for each  $\theta'$  in FOL-BC-AND( $KB, lhs, \text{UNIFY}(rhs, goal, \theta)$ ) do
      yield  $\theta'$ 

```

```

generator FOL-BC-AND( $KB, goals, \theta$ ) yields a substitution
  if  $\theta = \text{failure}$  then return
  else if LENGTH( $goals$ ) = 0 then yield  $\theta$ 
  else do
     $first, rest \leftarrow \text{FIRST}(goals), \text{REST}(goals)$ 
    for each  $\theta'$  in FOL-BC-OR( $KB, \text{SUBST}(\theta, first), \theta$ ) do
      for each  $\theta''$  in FOL-BC-AND( $KB, rest, \theta'$ ) do
        yield  $\theta''$ 

```

Figure 9.6 A simple backward-chaining algorithm for first-order knowledge bases.

```
procedure APPEND( $ax, y, az, continuation$ )  
   $trail \leftarrow$  GLOBAL-TRAIL-POINTER()  
  if  $ax = []$  and UNIFY( $y, az$ ) then CALL( $continuation$ )  
  RESET-TRAIL( $trail$ )  
   $a, x, z \leftarrow$  NEW-VARIABLE(), NEW-VARIABLE(), NEW-VARIABLE()  
  if UNIFY( $ax, [a \mid x]$ ) and UNIFY( $az, [a \mid z]$ ) then APPEND( $x, y, z, continuation$ )
```

Figure 9.8 Pseudocode representing the result of compiling the Append predicate. The function NEW-VARIABLE returns a new variable, distinct from all other variables used so far. The procedure CALL($continuation$) continues execution with the specified continuation.

10 CLASSICAL PLANNING

```

Init(At(C1, SFO) ∧ At(C2, JFK) ∧ At(P1, SFO) ∧ At(P2, JFK)
    ∧ Cargo(C1) ∧ Cargo(C2) ∧ Plane(P1) ∧ Plane(P2)
    ∧ Airport(JFK) ∧ Airport(SFO))
Goal(At(C1, JFK) ∧ At(C2, SFO))
Action(Load(c, p, a),
    PRECOND: At(c, a) ∧ At(p, a) ∧ Cargo(c) ∧ Plane(p) ∧ Airport(a)
    EFFECT: ¬ At(c, a) ∧ In(c, p))
Action(Unload(c, p, a),
    PRECOND: In(c, p) ∧ At(p, a) ∧ Cargo(c) ∧ Plane(p) ∧ Airport(a)
    EFFECT: At(c, a) ∧ ¬ In(c, p))
Action(Fly(p, from, to),
    PRECOND: At(p, from) ∧ Plane(p) ∧ Airport(from) ∧ Airport(to)
    EFFECT: ¬ At(p, from) ∧ At(p, to))

```

Figure 10.1 A PDDL description of an air cargo transportation planning problem.

```

Init(Tire(Flat) ∧ Tire(Spare) ∧ At(Flat, Axle) ∧ At(Spare, Trunk))
Goal(At(Spare, Axle))
Action(Remove(obj, loc),
    PRECOND: At(obj, loc)
    EFFECT: ¬ At(obj, loc) ∧ At(obj, Ground))
Action(PutOn(t, Axle),
    PRECOND: Tire(t) ∧ At(t, Ground) ∧ ¬ At(Flat, Axle)
    EFFECT: ¬ At(t, Ground) ∧ At(t, Axle))
Action(LeaveOvernight,
    PRECOND:
    EFFECT: ¬ At(Spare, Ground) ∧ ¬ At(Spare, Axle) ∧ ¬ At(Spare, Trunk)
           ∧ ¬ At(Flat, Ground) ∧ ¬ At(Flat, Axle) ∧ ¬ At(Flat, Trunk))

```

Figure 10.2 The simple spare tire problem.

```

Init(On(A, Table) ∧ On(B, Table) ∧ On(C, A)
    ∧ Block(A) ∧ Block(B) ∧ Block(C) ∧ Clear(B) ∧ Clear(C))
Goal(On(A, B) ∧ On(B, C))
Action(Move(b, x, y),
    PRECOND: On(b, x) ∧ Clear(b) ∧ Clear(y) ∧ Block(b) ∧ Block(y) ∧
        (b ≠ x) ∧ (b ≠ y) ∧ (x ≠ y),
    EFFECT: On(b, y) ∧ Clear(x) ∧ ¬On(b, x) ∧ ¬Clear(y))
Action(MoveToTable(b, x),
    PRECOND: On(b, x) ∧ Clear(b) ∧ Block(b) ∧ (b ≠ x),
    EFFECT: On(b, Table) ∧ Clear(x) ∧ ¬On(b, x))

```

Figure 10.3 A planning problem in the blocks world: building a three-block tower. One solution is the sequence [MoveToTable(C, A), Move(B, Table, C), Move(A, Table, B)].

```

Init(Have(Cake))
Goal(Have(Cake) ∧ Eaten(Cake))
Action(Eat(Cake)
    PRECOND: Have(Cake)
    EFFECT: ¬Have(Cake) ∧ Eaten(Cake))
Action(Bake(Cake)
    PRECOND: ¬Have(Cake)
    EFFECT: Have(Cake))

```

Figure 10.7 The “have cake and eat cake too” problem.

```

function GRAPHPLAN(problem) returns solution or failure
    graph ← INITIAL-PLANNING-GRAPH(problem)
    goals ← CONJUNCTS(problem.GOAL)
    nogoods ← an empty hash table
    for tl = 0 to ∞ do
        if goals all non-mutex in  $S_t$  of graph then
            solution ← EXTRACT-SOLUTION(graph, goals, NUMLEVELS(graph), nogoods)
            if solution ≠ failure then return solution
        if graph and nogoods have both leveled off then return failure
        graph ← EXPAND-GRAPH(graph, problem)

```

Figure 10.9 The GRAPHPLAN algorithm. GRAPHPLAN calls EXPAND-GRAPH to add a level until either a solution is found by EXTRACT-SOLUTION, or no solution is possible.

11 PLANNING AND ACTING IN THE REAL WORLD

```
Jobs({AddEngine1  $\prec$  AddWheels1  $\prec$  Inspect1},  
      {AddEngine2  $\prec$  AddWheels2  $\prec$  Inspect2})  
  
Resources(EngineHoists(1), WheelStations(1), Inspectors(2), LugNuts(500))  
  
Action(AddEngine1, DURATION:30,  
       USE:EngineHoists(1))  
Action(AddEngine2, DURATION:60,  
       USE:EngineHoists(1))  
Action(AddWheels1, DURATION:30,  
       CONSUME:LugNuts(20), USE:WheelStations(1))  
Action(AddWheels2, DURATION:15,  
       CONSUME:LugNuts(20), USE:WheelStations(1))  
Action(Inspecti, DURATION:10,  
       USE:Inspectors(1))
```

Figure 11.1 A job-shop scheduling problem for assembling two cars, with resource constraints. The notation $A \prec B$ means that action A must precede action B .

```

Refinement(Go(Home, SFO),
  STEPS: [Drive(Home, SFOLongTermParking),
          Shuttle(SFOLongTermParking, SFO)] )

Refinement(Go(Home, SFO),
  STEPS: [Taxi(Home, SFO)] )

Refinement(Navigate([a, b], [x, y]),
  PRECOND: a = x ∧ b = y
  STEPS: [] )

Refinement(Navigate([a, b], [x, y]),
  PRECOND: Connected([a, b], [a − 1, b])
  STEPS: [Left, Navigate([a − 1, b], [x, y])] )

Refinement(Navigate([a, b], [x, y]),
  PRECOND: Connected([a, b], [a + 1, b])
  STEPS: [Right, Navigate([a + 1, b], [x, y])] )

...

```

Figure 11.4 Definitions of possible refinements for two high-level actions: going to San Francisco airport and navigating in the vacuum world. In the latter case, note the recursive nature of the refinements and the use of preconditions.

function HIERARCHICAL-SEARCH(*problem*, *hierarchy*) **returns** a solution, or failure

```

frontier ← a FIFO queue with [Act] as the only element
loop do
  if EMPTY?(frontier) then return failure
  plan ← POP(frontier) /* chooses the shallowest plan in frontier */
  hla ← the first HLA in plan, or null if none
  prefix, suffix ← the action subsequences before and after hla in plan
  outcome ← RESULT(problem.INITIAL-STATE, prefix)
  if hla is null then /* so plan is primitive and outcome is its result */
    if outcome satisfies problem.GOAL then return plan
  else for each sequence in REFINEMENTS(hla, outcome, hierarchy) do
    frontier ← INSERT(APPEND(prefix, sequence, suffix), frontier)

```

Figure 11.5 A breadth-first implementation of hierarchical forward planning search. The initial plan supplied to the algorithm is [*Act*]. The REFINEMENTS function returns a set of action sequences, one for each refinement of the HLA whose preconditions are satisfied by the specified state, *outcome*.

```

function ANGELIC-SEARCH(problem, hierarchy, initialPlan) returns solution or fail
  frontier  $\leftarrow$  a FIFO queue with initialPlan as the only element
  loop do
    if EMPTY?(frontier) then return fail
    plan  $\leftarrow$  POP(frontier) /* chooses the shallowest node in frontier */
    if REACH+(problem.INITIAL-STATE, plan) intersects problem.GOAL then
      if plan is primitive then return plan /* REACH+ is exact for primitive plans */
      guaranteed  $\leftarrow$  REACH-(problem.INITIAL-STATE, plan)  $\cap$  problem.GOAL
      if guaranteed  $\neq \{ \}$  and MAKING-PROGRESS(plan, initialPlan) then
        finalState  $\leftarrow$  any element of guaranteed
        return DECOMPOSE(hierarchy, problem.INITIAL-STATE, plan, finalState)
    hla  $\leftarrow$  some HLA in plan
    prefix, suffix  $\leftarrow$  the action subsequences before and after hla in plan
    for each sequence in REFINEMENTS(hla, outcome, hierarchy) do
      frontier  $\leftarrow$  INSERT(APPEND(prefix, sequence, suffix), frontier)

```

```

function DECOMPOSE(hierarchy, s0, plan, sf) returns a solution
  solution  $\leftarrow$  an empty plan
  while plan is not empty do
    action  $\leftarrow$  REMOVE-LAST(plan)
    si  $\leftarrow$  a state in REACH-(s0, plan) such that sf  $\in$  REACH-(si, action)
    problem  $\leftarrow$  a problem with INITIAL-STATE = si and GOAL = sf
    solution  $\leftarrow$  APPEND(ANGELIC-SEARCH(problem, hierarchy, action), solution)
    sf  $\leftarrow$  si
  return solution

```

Figure 11.8 A hierarchical planning algorithm that uses angelic semantics to identify and commit to high-level plans that work while avoiding high-level plans that don't. The predicate MAKING-PROGRESS checks to make sure that we aren't stuck in an infinite regression of refinements. At top level, call ANGELIC-SEARCH with [*Act*] as the *initialPlan*.

```

Actors(A, B)
Init(At(A, LeftBaseline)  $\wedge$  At(B, RightNet)  $\wedge$ 
    Approaching(Ball, RightBaseline)  $\wedge$  Partner(A, B)  $\wedge$  Partner(B, A)
Goal(Returned(Ball)  $\wedge$  (At(a, RightNet)  $\vee$  At(a, LeftNet))
Action(Hit(actor, Ball),
    PRECOND:Approaching(Ball, loc)  $\wedge$  At(actor, loc)
    EFFECT:Returned(Ball))
Action(Go(actor, to),
    PRECOND:At(actor, loc)  $\wedge$  to  $\neq$  loc,
    EFFECT:At(actor, to)  $\wedge$   $\neg$  At(actor, loc))

```

Figure 11.10 The doubles tennis problem. Two actors *A* and *B* are playing together and can be in one of four locations: *LeftBaseline*, *RightBaseline*, *LeftNet*, and *RightNet*. The ball can be returned only if a player is in the right place. Note that each action must include the actor as an argument.

12 KNOWLEDGE REPRESENTATION

13 QUANTIFYING UNCERTAINTY

function DT-AGENT(*percept*) **returns** an *action*
persistent: *belief_state*, probabilistic beliefs about the current state of the world
 action, the agent's action

update *belief_state* based on *action* and *percept*
calculate outcome probabilities for actions,
 given action descriptions and current *belief_state*
select *action* with highest expected utility
 given probabilities of outcomes and utility information
return *action*

Figure 13.1 A decision-theoretic agent that selects rational actions.

14 PROBABILISTIC REASONING

```

function ENUMERATION-ASK( $X, \mathbf{e}, bn$ ) returns a distribution over  $X$ 
  inputs:  $X$ , the query variable
            $\mathbf{e}$ , observed values for variables  $\mathbf{E}$ 
            $bn$ , a Bayes net with variables  $\{X\} \cup \mathbf{E} \cup \mathbf{Y}$   /*  $\mathbf{Y}$  = hidden variables */

   $\mathbf{Q}(X) \leftarrow$  a distribution over  $X$ , initially empty
  for each value  $x_i$  of  $X$  do
     $\mathbf{Q}(x_i) \leftarrow$  ENUMERATE-ALL( $bn.VARS, \mathbf{e}_{x_i}$ )
    where  $\mathbf{e}_{x_i}$  is  $\mathbf{e}$  extended with  $X = x_i$ 
  return NORMALIZE( $\mathbf{Q}(X)$ )

```

```

function ENUMERATE-ALL( $vars, \mathbf{e}$ ) returns a real number
  if EMPTY?( $vars$ ) then return 1.0
   $Y \leftarrow$  FIRST( $vars$ )
  if  $Y$  has value  $y$  in  $\mathbf{e}$ 
    then return  $P(y \mid \text{parents}(Y)) \times$  ENUMERATE-ALL(REST( $vars$ ),  $\mathbf{e}$ )
  else return  $\sum_y P(y \mid \text{parents}(Y)) \times$  ENUMERATE-ALL(REST( $vars$ ),  $\mathbf{e}_y$ )
  where  $\mathbf{e}_y$  is  $\mathbf{e}$  extended with  $Y = y$ 

```

Figure 14.9 The enumeration algorithm for answering queries on Bayesian networks.

```

function ELIMINATION-ASK( $X, \mathbf{e}, bn$ ) returns a distribution over  $X$ 
  inputs:  $X$ , the query variable
            $\mathbf{e}$ , observed values for variables  $\mathbf{E}$ 
            $bn$ , a Bayesian network specifying joint distribution  $\mathbf{P}(X_1, \dots, X_n)$ 

   $factors \leftarrow []$ 
  for each  $var$  in ORDER( $bn.VARS$ ) do
     $factors \leftarrow$  [MAKE-FACTOR( $var, \mathbf{e}$ ) |  $factors$ ]
    if  $var$  is a hidden variable then  $factors \leftarrow$  SUM-OUT( $var, factors$ )
  return NORMALIZE(POINTWISE-PRODUCT( $factors$ ))

```

Figure 14.10 The variable elimination algorithm for inference in Bayesian networks.

```

function PRIOR-SAMPLE( $bn$ ) returns an event sampled from the prior specified by  $bn$ 
inputs:  $bn$ , a Bayesian network specifying joint distribution  $\mathbf{P}(X_1, \dots, X_n)$ 

 $\mathbf{x} \leftarrow$  an event with  $n$  elements
foreach variable  $X_i$  in  $X_1, \dots, X_n$  do
     $\mathbf{x}[i] \leftarrow$  a random sample from  $\mathbf{P}(X_i \mid \text{parents}(X_i))$ 
return  $\mathbf{x}$ 

```

Figure 14.12 A sampling algorithm that generates events from a Bayesian network. Each variable is sampled according to the conditional distribution given the values already sampled for the variable's parents.

```

function REJECTION-SAMPLING( $X, \mathbf{e}, bn, N$ ) returns an estimate of  $\mathbf{P}(X \mid \mathbf{e})$ 
inputs:  $X$ , the query variable
     $\mathbf{e}$ , observed values for variables  $\mathbf{E}$ 
     $bn$ , a Bayesian network
     $N$ , the total number of samples to be generated
local variables:  $\mathbf{N}$ , a vector of counts for each value of  $X$ , initially zero

for  $j = 1$  to  $N$  do
     $\mathbf{x} \leftarrow$  PRIOR-SAMPLE( $bn$ )
    if  $\mathbf{x}$  is consistent with  $\mathbf{e}$  then
         $\mathbf{N}[x] \leftarrow \mathbf{N}[x] + 1$  where  $x$  is the value of  $X$  in  $\mathbf{x}$ 
return NORMALIZE( $\mathbf{N}$ )

```

Figure 14.13 The rejection-sampling algorithm for answering queries given evidence in a Bayesian network.

```

function LIKELIHOOD-WEIGHTING( $X, \mathbf{e}, bn, N$ ) returns an estimate of  $\mathbf{P}(X|\mathbf{e})$ 
  inputs:  $X$ , the query variable
            $\mathbf{e}$ , observed values for variables  $\mathbf{E}$ 
            $bn$ , a Bayesian network specifying joint distribution  $\mathbf{P}(X_1, \dots, X_n)$ 
            $N$ , the total number of samples to be generated
  local variables:  $\mathbf{W}$ , a vector of weighted counts for each value of  $X$ , initially zero

  for  $j = 1$  to  $N$  do
     $\mathbf{x}, w \leftarrow \text{WEIGHTED-SAMPLE}(bn, \mathbf{e})$ 
     $\mathbf{W}[x] \leftarrow \mathbf{W}[x] + w$  where  $x$  is the value of  $X$  in  $\mathbf{x}$ 
  return NORMALIZE( $\mathbf{W}$ )

```

```

function WEIGHTED-SAMPLE( $bn, \mathbf{e}$ ) returns an event and a weight
   $w \leftarrow 1$ ;  $\mathbf{x} \leftarrow$  an event with  $n$  elements initialized from  $\mathbf{e}$ 
  foreach variable  $X_i$  in  $X_1, \dots, X_n$  do
    if  $X_i$  is an evidence variable with value  $x_i$  in  $\mathbf{e}$ 
      then  $w \leftarrow w \times P(X_i = x_i \mid \text{parents}(X_i))$ 
      else  $\mathbf{x}[i] \leftarrow$  a random sample from  $\mathbf{P}(X_i \mid \text{parents}(X_i))$ 
  return  $\mathbf{x}, w$ 

```

Figure 14.14 The likelihood-weighting algorithm for inference in Bayesian networks. In WEIGHTED-SAMPLE, each nonevidence variable is sampled according to the conditional distribution given the values already sampled for the variable's parents, while a weight is accumulated based on the likelihood for each evidence variable.

```

function GIBBS-ASK( $X, \mathbf{e}, bn, N$ ) returns an estimate of  $\mathbf{P}(X|\mathbf{e})$ 
  local variables:  $\mathbf{N}$ , a vector of counts for each value of  $X$ , initially zero
                    $\mathbf{Z}$ , the nonevidence variables in  $bn$ 
                    $\mathbf{x}$ , the current state of the network, initially copied from  $\mathbf{e}$ 

  initialize  $\mathbf{x}$  with random values for the variables in  $\mathbf{Z}$ 
  for  $j = 1$  to  $N$  do
    for each  $Z_i$  in  $\mathbf{Z}$  do
      set the value of  $Z_i$  in  $\mathbf{x}$  by sampling from  $\mathbf{P}(Z_i \mid \text{mb}(Z_i))$ 
     $\mathbf{N}[x] \leftarrow \mathbf{N}[x] + 1$  where  $x$  is the value of  $X$  in  $\mathbf{x}$ 
  return NORMALIZE( $\mathbf{N}$ )

```

Figure 14.15 The Gibbs sampling algorithm for approximate inference in Bayesian networks; this version cycles through the variables, but choosing variables at random also works.

15 PROBABILISTIC REASONING OVER TIME

```

function FORWARD-BACKWARD(ev, prior) returns a vector of probability distributions
  inputs: ev, a vector of evidence values for steps  $1, \dots, t$ 
           prior, the prior distribution on the initial state,  $\mathbf{P}(\mathbf{X}_0)$ 
  local variables: fv, a vector of forward messages for steps  $0, \dots, t$ 
                     b, a representation of the backward message, initially all 1s
                     sv, a vector of smoothed estimates for steps  $1, \dots, t$ 

  fv[0]  $\leftarrow$  prior
  for  $i = 1$  to  $t$  do
    fv[ $i$ ]  $\leftarrow$  FORWARD(fv[ $i - 1$ ], ev[ $i$ ])
  for  $i = t$  downto  $1$  do
    sv[ $i$ ]  $\leftarrow$  NORMALIZE(fv[ $i$ ]  $\times$  b)
    b  $\leftarrow$  BACKWARD(b, ev[ $i$ ])
  return sv

```

Figure 15.4 The forward–backward algorithm for smoothing: computing posterior probabilities of a sequence of states given a sequence of observations. The FORWARD and BACKWARD operators are defined by Equations (??) and (??), respectively.

```

function FIXED-LAG-SMOOTHING( $e_t, hmm, d$ ) returns a distribution over  $\mathbf{X}_{t-d}$ 
  inputs:  $e_t$ , the current evidence for time step  $t$ 
            $hmm$ , a hidden Markov model with  $S \times S$  transition matrix  $\mathbf{T}$ 
            $d$ , the length of the lag for smoothing
  persistent:  $t$ , the current time, initially 1
                 $\mathbf{f}$ , the forward message  $\mathbf{P}(X_t|e_{1:t})$ , initially  $hmm.PRIOR$ 
                 $\mathbf{B}$ , the  $d$ -step backward transformation matrix, initially the identity matrix
                 $e_{t-d:t}$ , double-ended list of evidence from  $t-d$  to  $t$ , initially empty
  local variables:  $\mathbf{O}_{t-d}, \mathbf{O}_t$ , diagonal matrices containing the sensor model information

  add  $e_t$  to the end of  $e_{t-d:t}$ 
   $\mathbf{O}_t \leftarrow$  diagonal matrix containing  $\mathbf{P}(e_t|X_t)$ 
  if  $t > d$  then
     $\mathbf{f} \leftarrow \text{FORWARD}(\mathbf{f}, e_t)$ 
    remove  $e_{t-d-1}$  from the beginning of  $e_{t-d:t}$ 
     $\mathbf{O}_{t-d} \leftarrow$  diagonal matrix containing  $\mathbf{P}(e_{t-d}|X_{t-d})$ 
     $\mathbf{B} \leftarrow \mathbf{O}_{t-d}^{-1} \mathbf{T}^{-1} \mathbf{B} \mathbf{O}_t$ 
  else  $\mathbf{B} \leftarrow \mathbf{B} \mathbf{O}_t$ 
   $t \leftarrow t + 1$ 
  if  $t > d$  then return  $\text{NORMALIZE}(\mathbf{f} \times \mathbf{B} \mathbf{1})$  else return null

```

Figure 15.6 An algorithm for smoothing with a fixed time lag of d steps, implemented as an online algorithm that outputs the new smoothed estimate given the observation for a new time step. Notice that the final output $\text{NORMALIZE}(\mathbf{f} \times \mathbf{B} \mathbf{1})$ is just $\alpha \mathbf{f} \times \mathbf{b}$, by Equation (??).

```

function PARTICLE-FILTERING( $\mathbf{e}, N, dbn$ ) returns a set of samples for the next time step
  inputs:  $\mathbf{e}$ , the new incoming evidence
            $N$ , the number of samples to be maintained
            $dbn$ , a DBN with prior  $\mathbf{P}(\mathbf{X}_0)$ , transition model  $\mathbf{P}(\mathbf{X}_1|\mathbf{X}_0)$ , sensor model  $\mathbf{P}(\mathbf{E}_1|\mathbf{X}_1)$ 
  persistent:  $S$ , a vector of samples of size  $N$ , initially generated from  $\mathbf{P}(\mathbf{X}_0)$ 
  local variables:  $W$ , a vector of weights of size  $N$ 

  for  $i = 1$  to  $N$  do
     $S[i] \leftarrow$  sample from  $\mathbf{P}(\mathbf{X}_1 | \mathbf{X}_0 = S[i])$  /* step 1 */
     $W[i] \leftarrow \mathbf{P}(\mathbf{e} | \mathbf{X}_1 = S[i])$  /* step 2 */
   $S \leftarrow \text{WEIGHTED-SAMPLE-WITH-REPLACEMENT}(N, S, W)$  /* step 3 */
  return  $S$ 

```

Figure 15.17 The particle filtering algorithm implemented as a recursive update operation with state (the set of samples). Each of the sampling operations involves sampling the relevant slice variables in topological order, much as in PRIOR-SAMPLE. The WEIGHTED-SAMPLE-WITH-REPLACEMENT operation can be implemented to run in $O(N)$ expected time. The step numbers refer to the description in the text.

16 MAKING SIMPLE DECISIONS

```
function INFORMATION-GATHERING-AGENT(percept) returns an action  
  persistent: D, a decision network  
  
  integrate percept into D  
   $j \leftarrow$  the value that maximizes  $VPI(E_j) / Cost(E_j)$   
  if  $VPI(E_j) > Cost(E_j)$   
    return REQUEST( $E_j$ )  
  else return the best action from D
```

Figure 16.9 Design of a simple information-gathering agent. The agent works by repeatedly selecting the observation with the highest information value, until the cost of the next observation is greater than its expected benefit.

17 MAKING COMPLEX DECISIONS

```

function VALUE-ITERATION( $mdp, \epsilon$ ) returns a utility function
  inputs:  $mdp$ , an MDP with states  $S$ , actions  $A(s)$ , transition model  $P(s' | s, a)$ ,
           rewards  $R(s)$ , discount  $\gamma$ 
            $\epsilon$ , the maximum error allowed in the utility of any state
  local variables:  $U, U'$ , vectors of utilities for states in  $S$ , initially zero
                      $\delta$ , the maximum change in the utility of any state in an iteration

  repeat
     $U \leftarrow U'; \delta \leftarrow 0$ 
    for each state  $s$  in  $S$  do
       $U'[s] \leftarrow R(s) + \gamma \max_{a \in A(s)} \sum_{s'} P(s' | s, a) U[s']$ 
      if  $|U'[s] - U[s]| > \delta$  then  $\delta \leftarrow |U'[s] - U[s]|$ 
  until  $\delta < \epsilon(1 - \gamma)/\gamma$ 
  return  $U$ 

```

Figure 17.4 The value iteration algorithm for calculating utilities of states. The termination condition is from Equation (??).


```

function POLICY-ITERATION(mdp) returns a policy
  inputs: mdp, an MDP with states  $S$ , actions  $A(s)$ , transition model  $P(s' | s, a)$ 
  local variables:  $U$ , a vector of utilities for states in  $S$ , initially zero
                   $\pi$ , a policy vector indexed by state, initially random

  repeat
     $U \leftarrow \text{POLICY-EVALUATION}(\pi, U, \text{mdp})$ 
     $\text{unchanged?} \leftarrow \text{true}$ 
    for each state  $s$  in  $S$  do
      if  $\max_{a \in A(s)} \sum_{s'} P(s' | s, a) U[s'] > \sum_{s'} P(s' | s, \pi[s]) U[s']$  then do
         $\pi[s] \leftarrow \operatorname{argmax}_{a \in A(s)} \sum_{s'} P(s' | s, a) U[s']$ 
         $\text{unchanged?} \leftarrow \text{false}$ 
  until  $\text{unchanged?}$ 
  return  $\pi$ 

```

Figure 17.7 The policy iteration algorithm for calculating an optimal policy.

```

function POMDP-VALUE-ITERATION(pomdp,  $\epsilon$ ) returns a utility function
  inputs: pomdp, a POMDP with states  $S$ , actions  $A(s)$ , transition model  $P(s' | s, a)$ ,
          sensor model  $P(e | s)$ , rewards  $R(s)$ , discount  $\gamma$ 
           $\epsilon$ , the maximum error allowed in the utility of any state
  local variables:  $U, U'$ , sets of plans  $p$  with associated utility vectors  $\alpha_p$ 

   $U' \leftarrow$  a set containing just the empty plan  $[\ ]$ , with  $\alpha_{[\ ]}(s) = R(s)$ 
  repeat
     $U \leftarrow U'$ 
     $U' \leftarrow$  the set of all plans consisting of an action and, for each possible next percept,
      a plan in  $U$  with utility vectors computed according to Equation (??)
     $U' \leftarrow \text{REMOVE-DOMINATED-PLANS}(U')$ 
  until  $\text{MAX-DIFFERENCE}(U, U') < \epsilon(1 - \gamma)/\gamma$ 
  return  $U$ 

```

Figure 17.9 A high-level sketch of the value iteration algorithm for POMDPs. The REMOVE-DOMINATED-PLANS step and MAX-DIFFERENCE test are typically implemented as linear programs.

18 LEARNING FROM EXAMPLES

```

function DECISION-TREE-LEARNING(examples, attributes, parent_examples) returns      a
tree
    if examples is empty then return PLURALITY-VALUE(parent_examples)
    else if all examples have the same classification then return the classification
    else if attributes is empty then return PLURALITY-VALUE(examples)
    else
         $A \leftarrow \operatorname{argmax}_{a \in \text{attributes}} \text{IMPORTANCE}(a, \text{examples})$ 
        tree  $\leftarrow$  a new decision tree with root test A
        for each value  $v_k$  of A do
            exs  $\leftarrow \{e : e \in \text{examples} \text{ and } e.A = v_k\}$ 
            subtree  $\leftarrow$  DECISION-TREE-LEARNING(exs, attributes − A, examples)
            add a branch to tree with label (A =  $v_k$ ) and subtree subtree
    return tree

```

Figure 18.4 The decision-tree learning algorithm. The function IMPORTANCE is described in Section ???. The function PLURALITY-VALUE selects the most common output value among a set of examples, breaking ties randomly.

function CROSS-VALIDATION-WRAPPER(*Learner*, *k*, *examples*) **returns** a hypothesis

local variables: *errT*, an array, indexed by *size*, storing training-set error rates
errV, an array, indexed by *size*, storing validation-set error rates
for *size* = 1 **to** ∞ **do**
 errT[*size*], *errV*[*size*] \leftarrow CROSS-VALIDATION(*Learner*, *size*, *k*, *examples*)
 if *errT* has converged **then do**
 best_size \leftarrow the value of *size* with minimum *errV*[*size*]
 return *Learner*(*best_size*, *examples*)

function CROSS-VALIDATION(*Learner*, *size*, *k*, *examples*) **returns** two values:
 average training set error rate, average validation set error rate

fold_errT \leftarrow 0; *fold_errV* \leftarrow 0
for *fold* = 1 **to** *k* **do**
 training_set, *validation_set* \leftarrow PARTITION(*examples*, *fold*, *k*)
 h \leftarrow *Learner*(*size*, *training_set*)
 fold_errT \leftarrow *fold_errT* + ERROR-RATE(*h*, *training_set*)
 fold_errV \leftarrow *fold_errV* + ERROR-RATE(*h*, *validation_set*)
return *fold_errT*/*k*, *fold_errV*/*k*

Figure 18.7 An algorithm to select the model that has the lowest error rate on validation data by building models of increasing complexity, and choosing the one with best empirical error rate on validation data. Here *errT* means error rate on the training data, and *errV* means error rate on the validation data. *Learner*(*size*, *examples*) returns a hypothesis whose complexity is set by the parameter *size*, and which is trained on the *examples*. PARTITION(*examples*, *fold*, *k*) splits *examples* into two subsets: a validation set of size N/k and a training set with all the other examples. The split is different for each value of *fold*.

function DECISION-LIST-LEARNING(*examples*) **returns** a decision list, or *failure*

if *examples* is empty **then return** the trivial decision list *No*
 t \leftarrow a test that matches a nonempty subset *examples_t* of *examples*
 such that the members of *examples_t* are all positive or all negative
 if there is no such *t* **then return** *failure*
 if the examples in *examples_t* are positive **then** *o* \leftarrow *Yes* **else** *o* \leftarrow *No*
 return a decision list with initial test *t* and outcome *o* and remaining tests given by
 DECISION-LIST-LEARNING(*examples* − *examples_t*)

Figure 18.10 An algorithm for learning decision lists.

```

function BACK-PROP-LEARNING(examples, network) returns a neural network
  inputs: examples, a set of examples, each with input vector x and output vector y
           network, a multilayer network with  $L$  layers, weights  $w_{i,j}$ , activation function  $g$ 
  local variables:  $\Delta$ , a vector of errors, indexed by network node

  repeat
    for each weight  $w_{i,j}$  in network do
       $w_{i,j} \leftarrow$  a small random number
    for each example (x, y) in examples do
      /* Propagate the inputs forward to compute the outputs */
      for each node  $i$  in the input layer do
         $a_i \leftarrow x_i$ 
      for  $\ell = 2$  to  $L$  do
        for each node  $j$  in layer  $\ell$  do
           $in_j \leftarrow \sum_i w_{i,j} a_i$ 
           $a_j \leftarrow g(in_j)$ 
      /* Propagate deltas backward from output layer to input layer */
      for each node  $j$  in the output layer do
         $\Delta[j] \leftarrow g'(in_j) \times (y_j - a_j)$ 
      for  $\ell = L - 1$  to  $1$  do
        for each node  $i$  in layer  $\ell$  do
           $\Delta[i] \leftarrow g'(in_i) \sum_j w_{i,j} \Delta[j]$ 
      /* Update every weight in network using deltas */
      for each weight  $w_{i,j}$  in network do
         $w_{i,j} \leftarrow w_{i,j} + \alpha \times a_i \times \Delta[j]$ 
  until some stopping criterion is satisfied
  return network

```

Figure 18.23 The back-propagation algorithm for learning in multilayer networks.

```

function ADABOOST(examples, L, K) returns a weighted-majority hypothesis
  inputs: examples, set of  $N$  labeled examples  $(x_1, y_1), \dots, (x_N, y_N)$ 
           L, a learning algorithm
           K, the number of hypotheses in the ensemble
  local variables: w, a vector of  $N$  example weights, initially  $1/N$ 
                     h, a vector of  $K$  hypotheses
                     z, a vector of  $K$  hypothesis weights

  for  $k = 1$  to  $K$  do
    h[ $k$ ]  $\leftarrow L(\textit{examples}, \mathbf{w})$ 
    error  $\leftarrow 0$ 
    for  $j = 1$  to  $N$  do
      if h[ $k$ ]( $x_j$ )  $\neq y_j$  then error  $\leftarrow \textit{error} + \mathbf{w}[j]$ 
    for  $j = 1$  to  $N$  do
      if h[ $k$ ]( $x_j$ )  $= y_j$  then  $\mathbf{w}[j] \leftarrow \mathbf{w}[j] \cdot \textit{error} / (1 - \textit{error})$ 
    w  $\leftarrow \text{NORMALIZE}(\mathbf{w})$ 
    z[ $k$ ]  $\leftarrow \log(1 - \textit{error}) / \textit{error}$ 
  return WEIGHTED-MAJORITY(h, z)

```

Figure 18.33 The ADABOOST variant of the boosting method for ensemble learning. The algorithm generates hypotheses by successively reweighting the training examples. The function WEIGHTED-MAJORITY generates a hypothesis that returns the output value with the highest vote from the hypotheses in **h**, with votes weighted by **z**.

19 KNOWLEDGE IN LEARNING

```
function CURRENT-BEST-LEARNING(examples, h) returns a hypothesis or fail
  if examples is empty then
    return h
  e ← FIRST(examples)
  if e is consistent with h then
    return CURRENT-BEST-LEARNING(REST(examples), h)
  else if e is a false positive for h then
    for each h' in specializations of h consistent with examples seen so far do
      h'' ← CURRENT-BEST-LEARNING(REST(examples), h')
      if h'' ≠ fail then return h''
  else if e is a false negative for h then
    for each h' in generalizations of h consistent with examples seen so far do
      h'' ← CURRENT-BEST-LEARNING(REST(examples), h')
      if h'' ≠ fail then return h''
  return fail
```

Figure 19.2 The current-best-hypothesis learning algorithm. It searches for a consistent hypothesis that fits all the examples and backtracks when no consistent specialization/generalization can be found. To start the algorithm, any hypothesis can be passed in; it will be specialized or gneralized as needed.

```

function VERSION-SPACE-LEARNING(examples) returns a version space
  local variables:  $V$ , the version space: the set of all hypotheses

   $V \leftarrow$  the set of all hypotheses
  for each example  $e$  in examples do
    if  $V$  is not empty then  $V \leftarrow$  VERSION-SPACE-UPDATE( $V, e$ )
  return  $V$ 

```

```

function VERSION-SPACE-UPDATE( $V, e$ ) returns an updated version space
   $V \leftarrow \{h \in V : h \text{ is consistent with } e\}$ 

```

Figure 19.3 The version space learning algorithm. It finds a subset of V that is consistent with all the *examples*.

```

function MINIMAL-CONSISTENT-DET( $E, A$ ) returns a set of attributes
  inputs:  $E$ , a set of examples
            $A$ , a set of attributes, of size  $n$ 

  for  $i = 0$  to  $n$  do
    for each subset  $A_i$  of  $A$  of size  $i$  do
      if CONSISTENT-DET?( $A_i, E$ ) then return  $A_i$ 

```

```

function CONSISTENT-DET?( $A, E$ ) returns a truth value
  inputs:  $A$ , a set of attributes
            $E$ , a set of examples
  local variables:  $H$ , a hash table

  for each example  $e$  in  $E$  do
    if some example in  $H$  has the same values as  $e$  for the attributes  $A$ 
      but a different classification then return false
    store the class of  $e$  in  $H$ , indexed by the values for attributes  $A$  of the example  $e$ 
  return true

```

Figure 19.8 An algorithm for finding a minimal consistent determination.

```

function FOIL(examples, target) returns a set of Horn clauses
  inputs: examples, set of examples
           target, a literal for the goal predicate
  local variables: clauses, set of clauses, initially empty

  while examples contains positive examples do
    clause  $\leftarrow$  NEW-CLAUSE(examples, target)
    remove positive examples covered by clause from examples
    add clause to clauses
  return clauses

```

```

function NEW-CLAUSE(examples, target) returns a Horn clause
  local variables: clause, a clause with target as head and an empty body
                   l, a literal to be added to the clause
                   extended_examples, a set of examples with values for new variables

  extended_examples  $\leftarrow$  examples
  while extended_examples contains negative examples do
    l  $\leftarrow$  CHOOSE-LITERAL(NEW-LITERALS(clause), extended_examples)
    append l to the body of clause
    extended_examples  $\leftarrow$  set of examples created by applying EXTEND-EXAMPLE
      to each example in extended_examples
  return clause

```

```

function EXTEND-EXAMPLE(example, literal) returns a set of examples
  if example satisfies literal
    then return the set of examples created by extending example with
      each possible constant value for each new variable in literal
  else return the empty set

```

Figure 19.12 Sketch of the FOIL algorithm for learning sets of first-order Horn clauses from examples. NEW-LITERALS and CHOOSE-LITERAL are explained in the text.

20 LEARNING PROBABILISTIC MODELS

21 REINFORCEMENT LEARNING

```

function PASSIVE-ADP-AGENT(percept) returns an action
  inputs: percept, a percept indicating the current state  $s'$  and reward signal  $r'$ 
  persistent:  $\pi$ , a fixed policy
               mdp, an MDP with model  $P$ , rewards  $R$ , discount  $\gamma$ 
                $U$ , a table of utilities, initially empty
                $N_{sa}$ , a table of frequencies for state–action pairs, initially zero
                $N_{s'|sa}$ , a table of outcome frequencies given state–action pairs, initially zero
                $s, a$ , the previous state and action, initially null

  if  $s'$  is new then  $U[s'] \leftarrow r'; R[s'] \leftarrow r'$ 
  if  $s$  is not null then
    increment  $N_{sa}[s, a]$  and  $N_{s'|sa}[s', s, a]$ 
    for each  $t$  such that  $N_{s'|sa}[t, s, a]$  is nonzero do
       $P(t | s, a) \leftarrow N_{s'|sa}[t, s, a] / N_{sa}[s, a]$ 
     $U \leftarrow \text{POLICY-EVALUATION}(\pi, U, mdp)$ 
  if  $s'.\text{TERMINAL?}$  then  $s, a \leftarrow \text{null}$  else  $s, a \leftarrow s', \pi[s']$ 
  return  $a$ 

```

Figure 21.2 A passive reinforcement learning agent based on adaptive dynamic programming. The POLICY-EVALUATION function solves the fixed-policy Bellman equations, as described on page ??.

```

function PASSIVE-TD-AGENT(percept) returns an action
  inputs: percept, a percept indicating the current state  $s'$  and reward signal  $r'$ 
  persistent:  $\pi$ , a fixed policy
                $U$ , a table of utilities, initially empty
                $N_s$ , a table of frequencies for states, initially zero
                $s, a, r$ , the previous state, action, and reward, initially null

  if  $s'$  is new then  $U[s'] \leftarrow r'$ 
  if  $s$  is not null then
    increment  $N_s[s]$ 
     $U[s] \leftarrow U[s] + \alpha(N_s[s])(r + \gamma U[s'] - U[s])$ 
  if  $s'.\text{TERMINAL?}$  then  $s, a, r \leftarrow \text{null}$  else  $s, a, r \leftarrow s', \pi[s'], r'$ 
  return  $a$ 

```

Figure 21.4 A passive reinforcement learning agent that learns utility estimates using temporal differences. The step-size function $\alpha(n)$ is chosen to ensure convergence, as described in the text.

```

function Q-LEARNING-AGENT(percept) returns an action
  inputs: percept, a percept indicating the current state  $s'$  and reward signal  $r'$ 
  persistent:  $Q$ , a table of action values indexed by state and action, initially zero
                $N_{sa}$ , a table of frequencies for state–action pairs, initially zero
                $s, a, r$ , the previous state, action, and reward, initially null

  if  $\text{TERMINAL?}(s)$  then  $Q[s, \text{None}] \leftarrow r'$ 
  if  $s$  is not null then
    increment  $N_{sa}[s, a]$ 
     $Q[s, a] \leftarrow Q[s, a] + \alpha(N_{sa}[s, a])(r + \gamma \max_{a'} Q[s', a'] - Q[s, a])$ 
     $s, a, r \leftarrow s', \text{argmax}_{a'} f(Q[s', a'], N_{sa}[s', a']), r'$ 
  return  $a$ 

```

Figure 21.8 An exploratory Q-learning agent. It is an active learner that learns the value $Q(s, a)$ of each action in each situation. It uses the same exploration function f as the exploratory ADP agent, but avoids having to learn the transition model because the Q-value of a state can be related directly to those of its neighbors.

22 NATURAL LANGUAGE PROCESSING

function HITS(*query*) **returns** *pages* with hub and authority numbers

```
pages ← EXPAND-PAGES(RELEVANT-PAGES(query))
for each p in pages do
  p.AUTHORITY ← 1
  p.HUB ← 1
repeat until convergence do
  for each p in pages do
    p.AUTHORITY ←  $\sum_i \text{INLINK}_i(p).\text{HUB}$ 
    p.HUB ←  $\sum_i \text{OUTLINK}_i(p).\text{AUTHORITY}$ 
  NORMALIZE(pages)
return pages
```

Figure 22.1 The HITS algorithm for computing hubs and authorities with respect to a query. RELEVANT-PAGES fetches the pages that match the query, and EXPAND-PAGES adds in every page that links to or is linked from one of the relevant pages. NORMALIZE divides each page's score by the sum of the squares of all pages' scores (separately for both the authority and hubs scores).

23 NATURAL LANGUAGE FOR COMMUNICATION

```

function CYK-PARSE(words, grammar) returns P, a table of probabilities

  N ← LENGTH(words)
  M ← the number of nonterminal symbols in grammar
  P ← an array of size [M, N, N], initially all 0
  /* Insert lexical rules for each word */
  for i = 1 to N do
    for each rule of form (X → wordsi [p]) do
      P[X, i, 1] ← p
  /* Combine first and second parts of right-hand sides of rules, from short to long */
  for length = 2 to N do
    for start = 1 to N − length + 1 do
      for len1 = 1 to N − 1 do
        len2 ← length − len1
        for each rule of the form (X → Y Z [p]) do
          P[X, start, length] ← MAX(P[X, start, length],
                                     P[Y, start, len1] × P[Z, start + len1, len2] × p)
  return P

```

Figure 23.4 The CYK algorithm for parsing. Given a sequence of words, it finds the most probable derivation for the whole sequence and for each subsequence. It returns the whole table, *P*, in which an entry *P*[*X*, *start*, *len*] is the probability of the most probable *X* of length *len* starting at position *start*. If there is no *X* of that size at that location, the probability is 0.

```

[ [S [NP-SBJ-2 Her eyes]
  [VP were
    [VP glazed
      [NP *-2]
      [SBAR-ADV as if
        [S [NP-SBJ she]
          [VP did n't
            [VP [VP hear [NP *-1]]
              or
              [VP [ADVP even] see [NP *-1]]
              [NP-1 him]]]]]]]]]]
  .]

```

Figure 23.5 Annotated tree for the sentence “Her eyes were glazed as if she didn’t hear or even see him.” from the Penn Treebank. Note that in this grammar there is a distinction between an object noun phrase (*NP*) and a subject noun phrase (*NP-SBJ*). Note also a grammatical phenomenon we have not covered yet: the movement of a phrase from one part of the tree to another. This tree analyzes the phrase “hear or even see him” as consisting of two constituent *VP*s, [VP hear [NP *-1]] and [VP [ADVP even] see [NP *-1]], both of which have a missing object, denoted *-1, which refers to the *NP* labeled elsewhere in the tree as [NP-1 him].

24 PERCEPTION

25 ROBOTICS

```

function MONTE-CARLO-LOCALIZATION( $a, z, N, P(X'|X, v, \omega), P(z|z^*), m$ ) returns
a set of samples for the next time step
  inputs:  $a$ , robot velocities  $v$  and  $\omega$ 
            $z$ , range scan  $z_1, \dots, z_M$ 
            $P(X'|X, v, \omega)$ , motion model
            $P(z|z^*)$ , range sensor noise model
            $m$ , 2D map of the environment
  persistent:  $S$ , a vector of samples of size  $N$ 
  local variables:  $W$ , a vector of weights of size  $N$ 
                     $S'$ , a temporary vector of particles of size  $N$ 
                     $W'$ , a vector of weights of size  $N$ 

  if  $S$  is empty then      /* initialization phase */
    for  $i = 1$  to  $N$  do
       $S[i] \leftarrow$  sample from  $P(X_0)$ 
    for  $i = 1$  to  $N$  do /* update cycle */
       $S'[i] \leftarrow$  sample from  $P(X'|X = S[i], v, \omega)$ 
       $W'[i] \leftarrow 1$ 
      for  $j = 1$  to  $M$  do
         $z^* \leftarrow$  RAYCAST( $j, X = S'[i], m$ )
         $W'[i] \leftarrow W'[i] \cdot P(z_j | z^*)$ 
       $S \leftarrow$  WEIGHTED-SAMPLE-WITH-REPLACEMENT( $N, S', W'$ )
  return  $S$ 

```

Figure 25.9 A Monte Carlo localization algorithm using a range-scan sensor model with independent noise.

26 PHILOSOPHICAL FOUNDATIONS

27 AI: THE PRESENT AND FUTURE

28 MATHEMATICAL BACKGROUND

29

NOTES ON LANGUAGES AND ALGORITHMS

```
generator POWERS-OF-2() yields ints
```

```
   $i \leftarrow 1$ 
```

```
  while true do
```

```
    yield  $i$ 
```

```
     $i \leftarrow 2 \times i$ 
```

```
for  $p$  in POWERS-OF-2() do
```

```
  PRINT( $p$ )
```

Figure 29.1 Example of a generator function and its invocation within a loop.